Aging Rules: What Does the Past Tell About the Future in MANET?

Han Cai, Do Young Eun

Department of Electrical and Computer Engineering North Carolina State University May 19, 2009

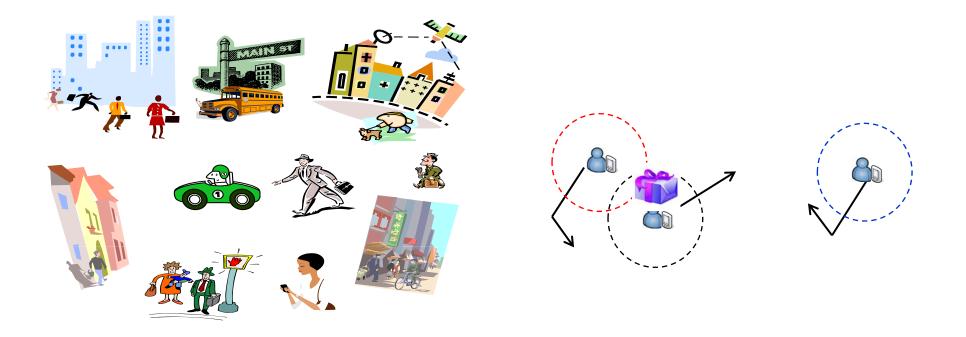




Intermittently connected mobile ad-hoc network: packet transmission through exploring the node mobility

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Intermittently connected mobile ad-hoc network: packet transmission through exploring the node mobility

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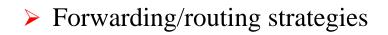


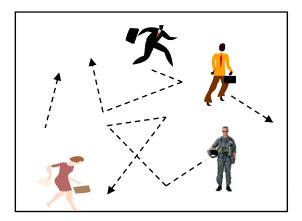
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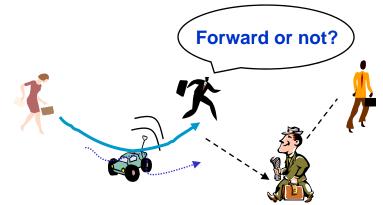


- Performance decided by:
 - Underlying mobility patterns
 - Real traces: realistic for any specific scenario
 - Synthetic mobility models: tractable analysis and design over different mobility settings in a controlled and repeatable manner





Random Mobility Pattern



Forwarding Strategy



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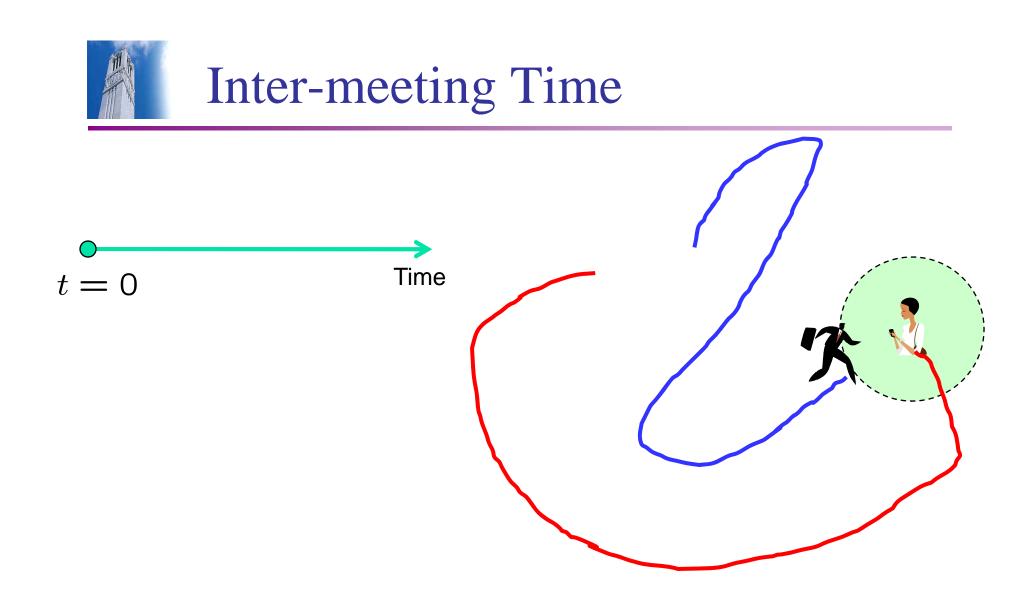






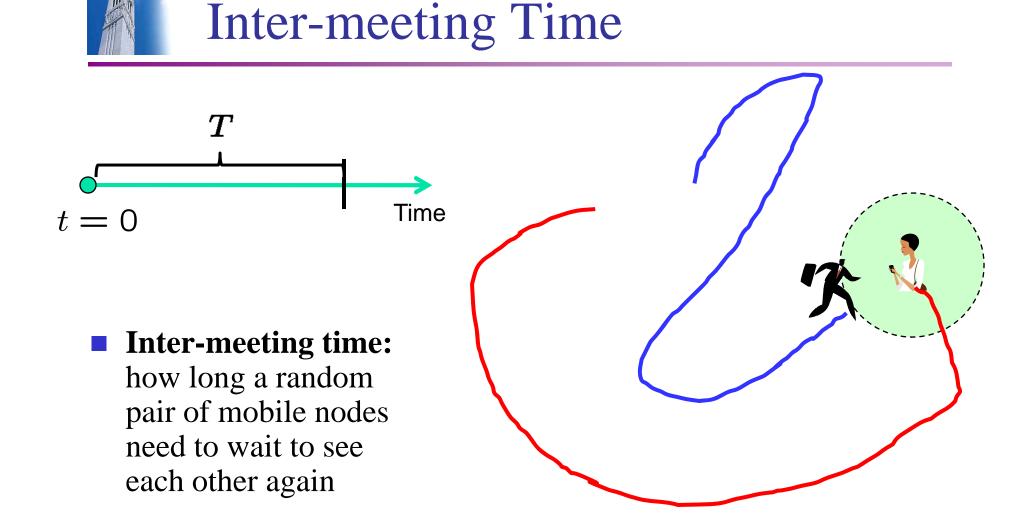
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Two Separate Approaches

Examples of analysis based on exponential intermeeting time assumption

M. Grossglauser and D. N. C. Tse. Infocom, 2001.

R. Groenevelt, P. Nain, and G. Koole. Sigmetrics, 2004.

G. Sharma, R. Mazumdar, and N. B. Shroff . *Infocom 2006*.

T. Spyropoulos, K. Psounis, and C. Raghavendra. *ToN* 2008.

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Examples of analysis based on non-exponential intermeeting time

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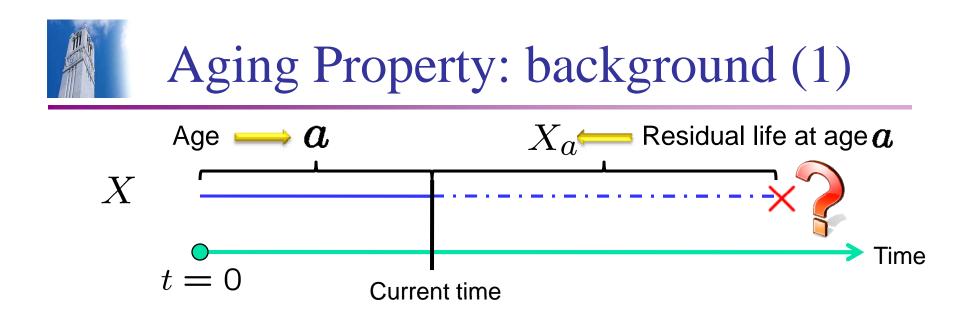
T. Karagiannis, J.-Y. Le Boudec, and M. Vojnovic. *Mobicom*, 2007.

Han Cai and Do Young Eun. MobiHoc, 2008

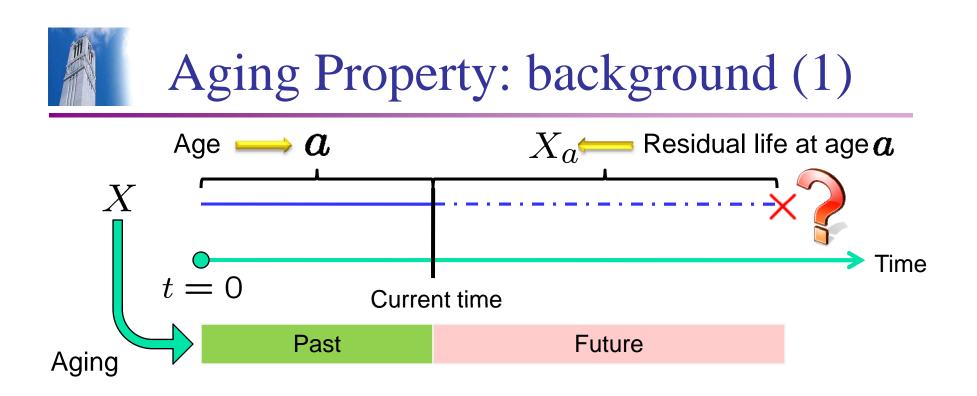
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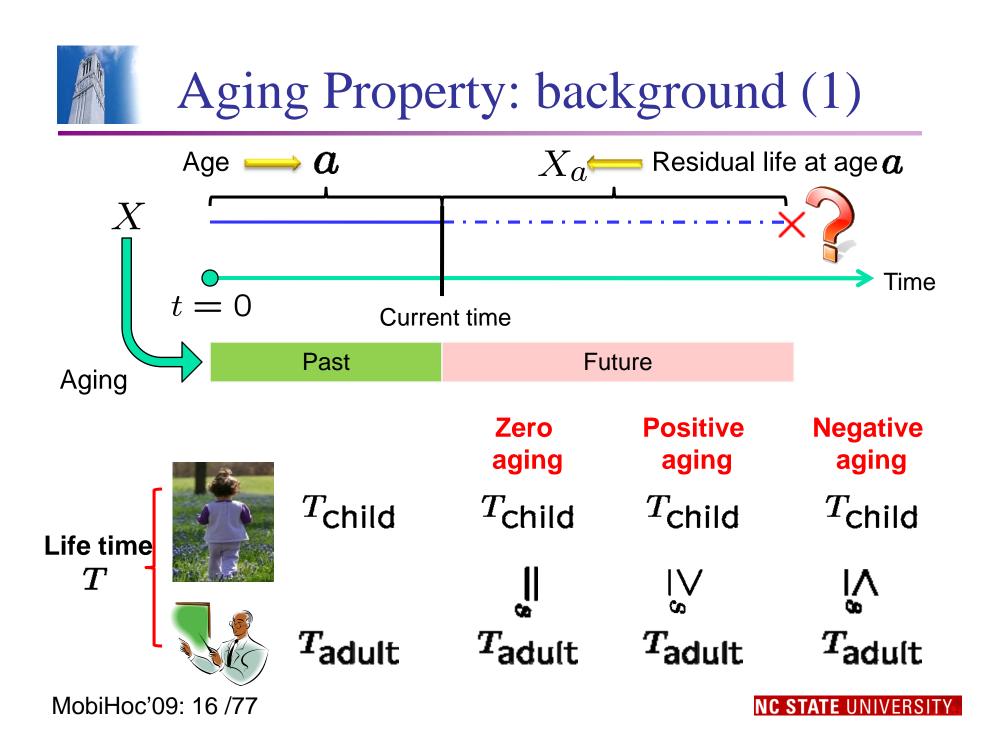














 $\blacksquare X_a$ decreases in a in the sense of stochastic ordering

 $\mathbb{P}\{X_{a1} \ge x\} \le \mathbb{P}\{X_{a2} \ge x\}, \text{ i.e., } X_{a1} \le_{st} X_{a2}, \forall a1 \ge a2$

- > In previous example: the child lives longer than the adult
- Necessary and sufficient condition for such ordering: Increasing Failure Rate (IFR)

$$r(x) = \mathbb{P}\{X = x\} / \mathbb{P}\{X \ge x\}$$

Probability of life ends at $oldsymbol{x}$ when it has survived up to $oldsymbol{x}$

> Other variants exists

Positive aging in weaker sense than IFR

> New Better then Used (NBU): $X_a \leq_{st} X_0$

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- > In previous example: the child lives longer than the adult
- Necessary and sufficient condition for such ordering: Decreasing Failure Rate (DFR)

$$r(x) = \mathbb{P}\{X = x\} / \mathbb{P}\{X \ge x\}$$

Probability of life ends at $oldsymbol{x}$ when it has survived up to $oldsymbol{x}$

> Other variants exists

Negative aging in weaker sense than DFR

> New Worse then Used (NWU): $X_a \ge_{st} X_0$

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Examples of analysis based on exponential intermeeting time assumption

M. Grossglauser and D. N. C. Tse. Infocom, 2001.

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Examples of analysis based on non-exponential intermeeting time

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Han Cai and Do Young Eun. *MobiCom*, 2007

Han Cai and Do Young Eun. MobiHoc, 2008

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aging Han Cai and Do Young Eun. *MobiCom*, 2007

Han Cai and Do Young Eun. MobiHoc, 2008

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What sacrifice have we made for simplicity?

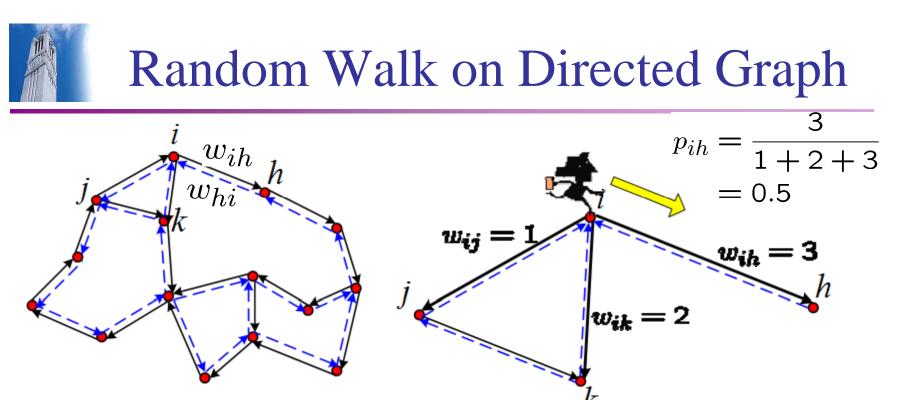
Is non-exponential inter-meeting time purely a disaster for MANET performance analysis and design?

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- Mobility Patterns with Zero/Negative/Positive Aging Intermeeting Time
 - Zero/Negative/Positive aging (CFR/DFR/IFR&NBU)
 - Negative/positive aging: under synthetic mobility models
- Performance Comparison: Non-exponential Inter-meeting time vs. Exponential Counterpart
- Aging in Forwarding/Routing





- Our definition of each class of models: $\{w_{ij}\}$, or $\{p_{ij}\}$
 - Focus: mobility features giving rise to unique aging property
 - > Assumptions:
 - -Connection: weakly connected, connected, 2-connected
 - -Non-bipartite

Difficulty of Aging Property Study

- Existing analysis on non-exponential inter-meeting time: current status
 - Head/tail behavior: the behavior of inter-meeting time distribution at small/large t [1, 2, 3, 4]
 - First-order behavior: average inter-meeting time [4]
 - [1] A. Chaintreau, P. Hui, J. Crowcroft, C. Diot, R. Gass, and J. Scott. Impact of human mobility on the design of opportunistic forwarding algorithms. In IEEE INFOCOM, Barcelona, Catalunya, SPAIN, 2006.
 - [2] Han Cai and Do Young Eun. Crossing Over the Bounded Domain: From Exponential to Power-law Intermeeting Time in MANET. In ACM MobiCom, Montreal, Canada, Sept. 2007
 - [3] T. Karagiannis, J.-Y. Le Boudec, and M. Vojnovic. Power law and exponential decay of inter contact times between mobile devices. In ACM Mobicom, Montreal, Canada, Sept. 2007
 - [4] Han Cai and Do Young Eun. Toward Stochastic Anatomy of Inter-meeting Time Distribution under General Mobility Models. In ACM MobiHoc, Hong Kong SAR, China, May 2008.

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- Our analysis on the aging property

 $r(t) = \mathbb{P}\{T = t\} / \mathbb{P}\{T \ge t\}$ increases (decreases) in *all* t?

 $\mathbb{P}\{T \ge t + \tau\} \le (\ge) \mathbb{P}\{T \ge t\} \mathbb{P}\{T \ge \tau\} \text{ holds for } all \ t \text{ and } \tau ?$

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- Existing analysis on non-exponential inter-meeting time: current status
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 - First-order behavior: average inter-meeting time [4]
- Our analysis on the aging property
 - Characteristics of relative mobility vs. aging: Inter-meeting of a random walker to a static reference site (home site)

 $r(t) = \mathbb{P}\{T = t\} / \mathbb{P}\{T \ge t\}$ increases (decreases) in *all* t?

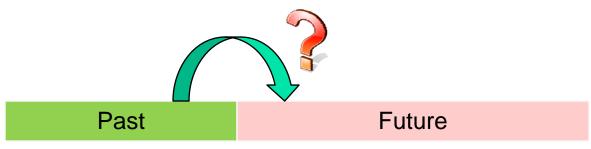
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Aging: the Power to Predict **Future** From the **Past** Information

■ The past and the future are tied with each other.

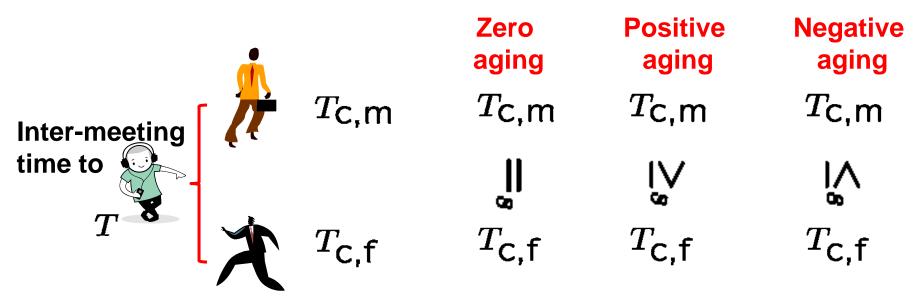






Aging: the Power to Predict **Future** From the **Past** Information

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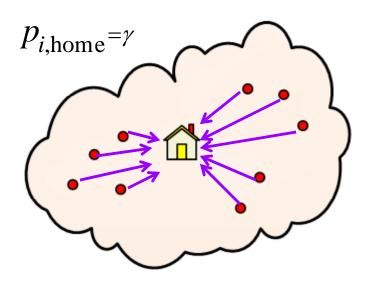
Relationship between the past and the future? What sacrifice have we made when ignoring the tie between the past and the future for simplicity? -- Our analysis will tell

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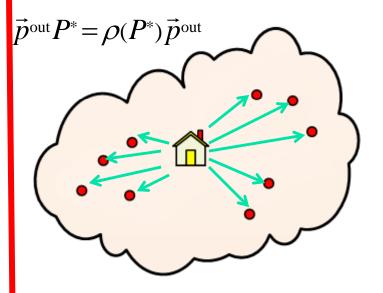
Zero-aging: Mobility Model Class 1

• Key feature: *small world* around the home site



- Subclass 1: homogeneous in-home condition
 - Special case: i.i.d. model

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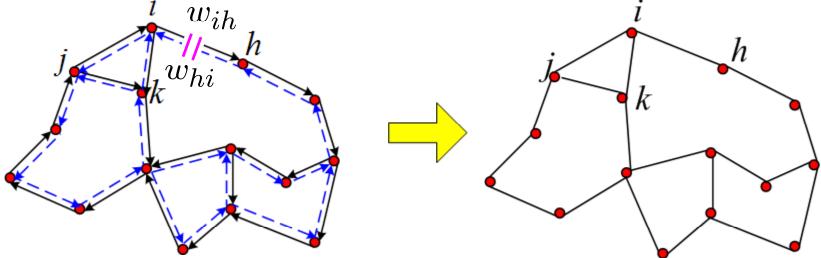
Subclass 2: out-home condition

Negative-aging: Mobility Model Class 2

Any random walk on undirected graph

> Time reversible Markov Chain $\pi_i p_{ij} = \pi_j p_{ji}$

Key feature: *undirected* graph



✓ Zero aging: independent age and residual life

✓ Negative aging: larger age → larger residual life. Dependence brings opportunity to design (*predict the future*)

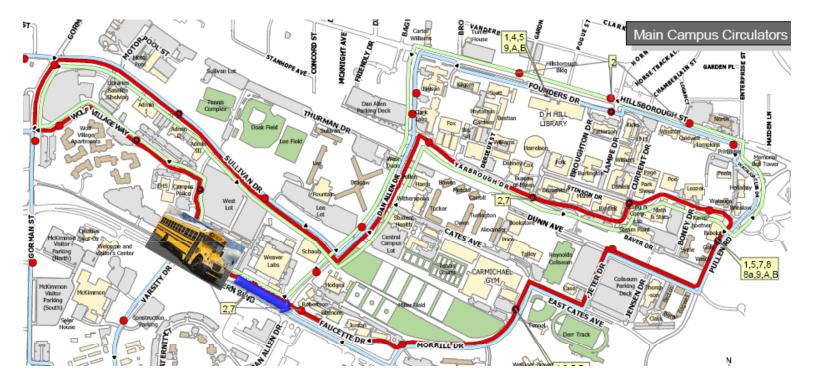
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- Examples of negative-aging class of mobility models:
 - > 1-D, 2-D random walk on grid
- In real traces and synthetic mobility models:
 - Power-law or mixture (power-law + exponential) behavior : suggests negative aging property [1, 2, 3]
 - [4] compared non-exponential inter-meeting times, which actually all have negative aging
 - [1] A. Chaintreau, P. Hui, J. Crowcroft, C. Diot, R. Gass, and J. Scott. Impact of human mobility on the design of opportunistic forwarding algorithms. In IEEE INFOCOM, Barcelona, Catalunya, SPAIN, 2006.
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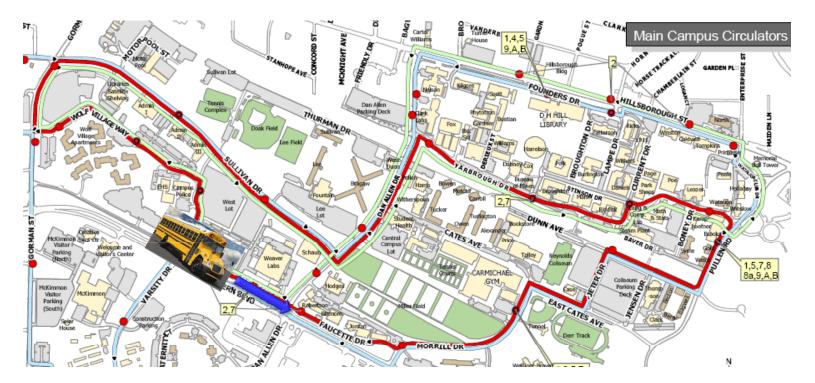
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■ Bus routes (http://www2.acs.ncsu.edu/trans/transportation/wolfline/)





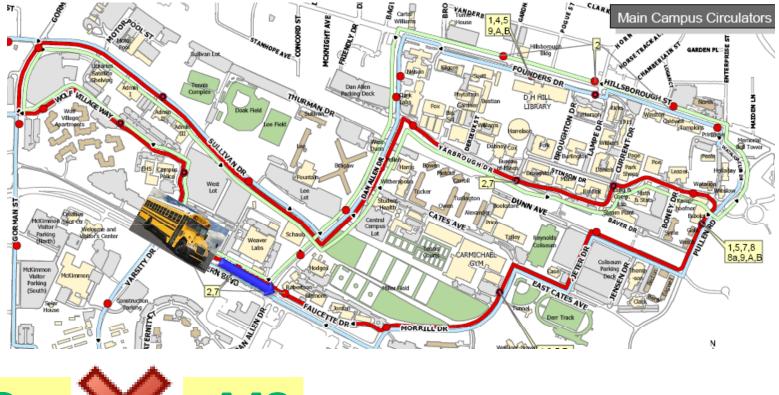
Bus routes (http://www2.acs.ncsu.edu/trans/transportation/wolfline/)



Small World?

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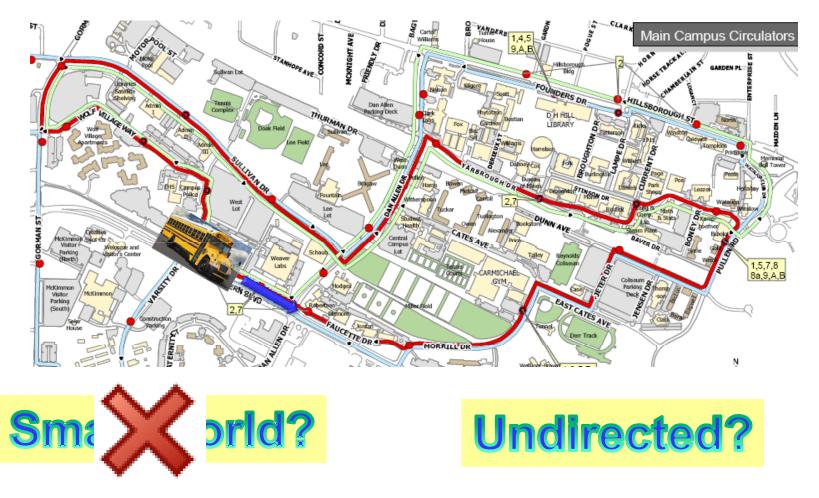




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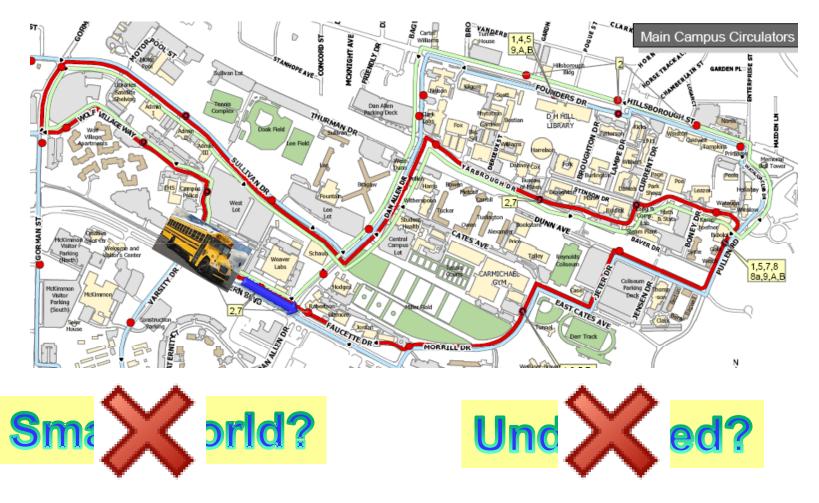


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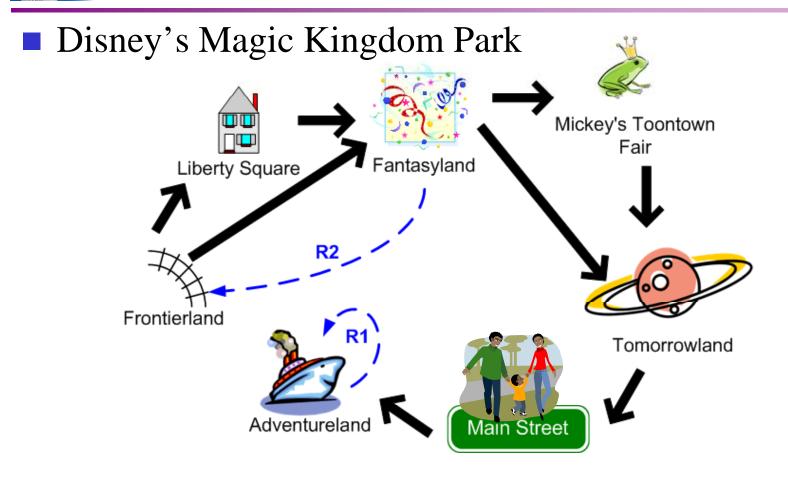


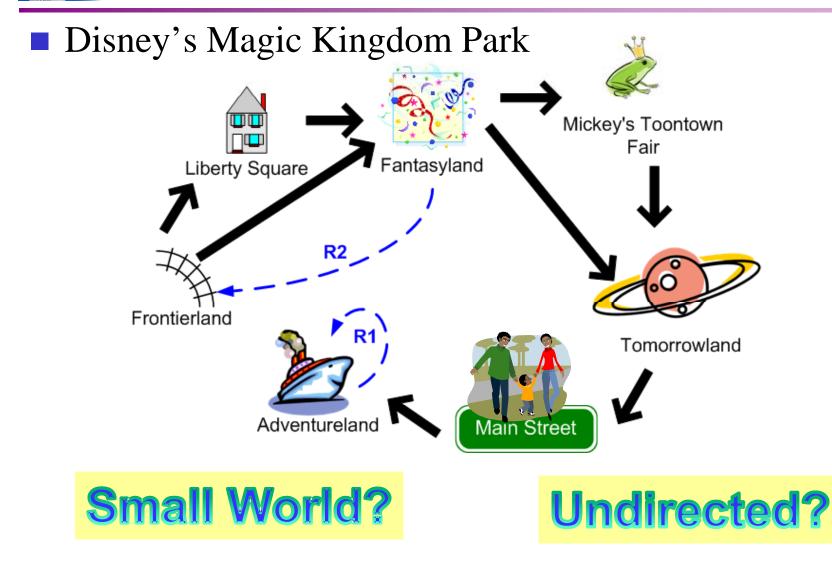
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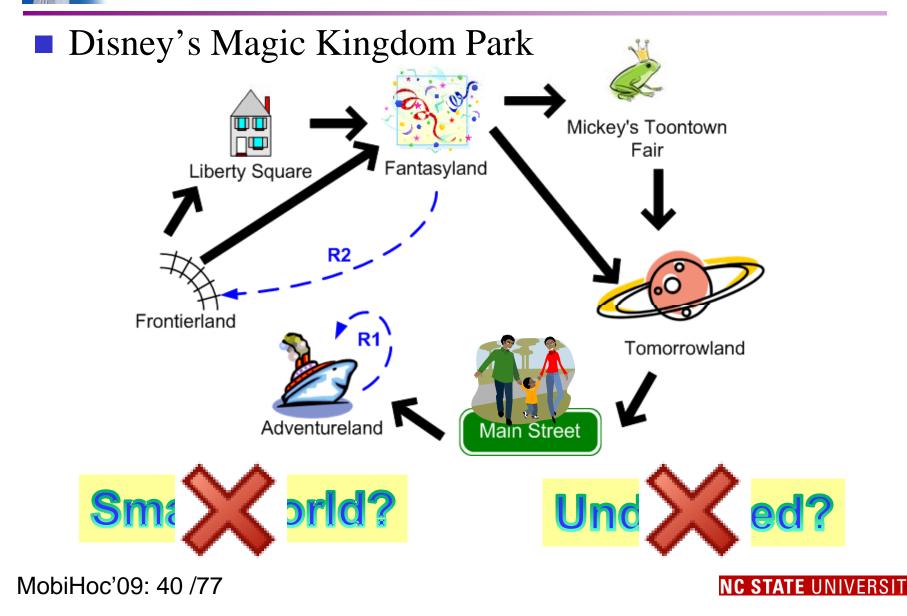


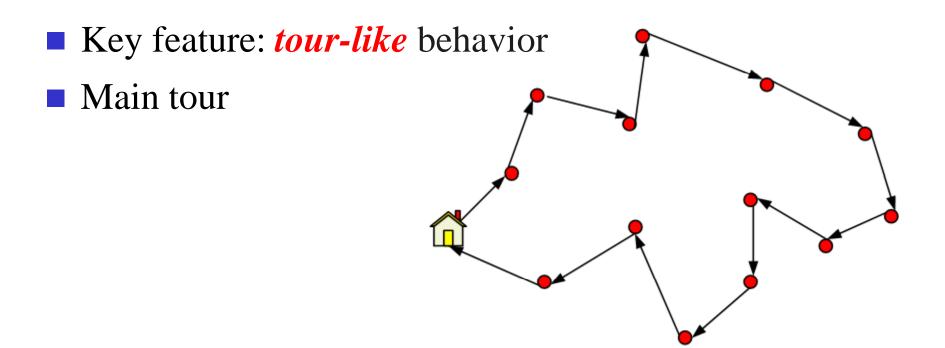
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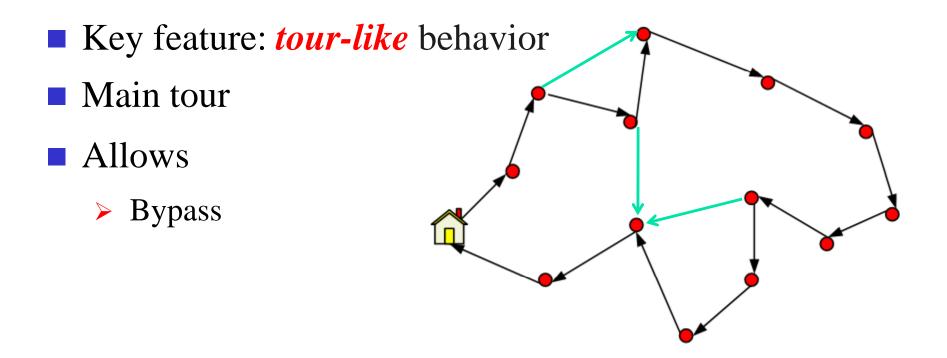
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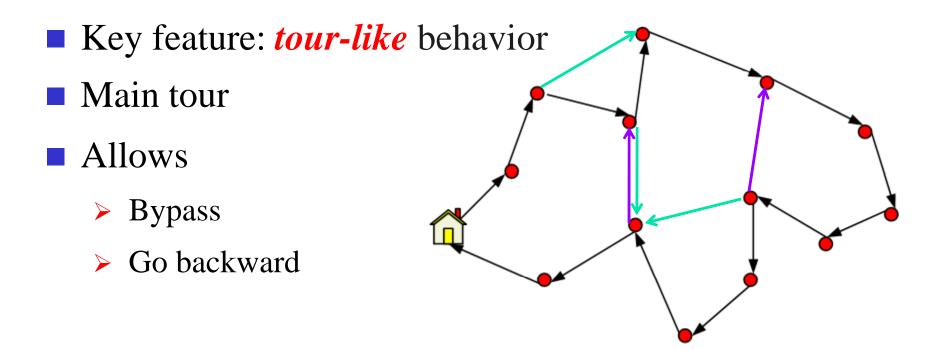




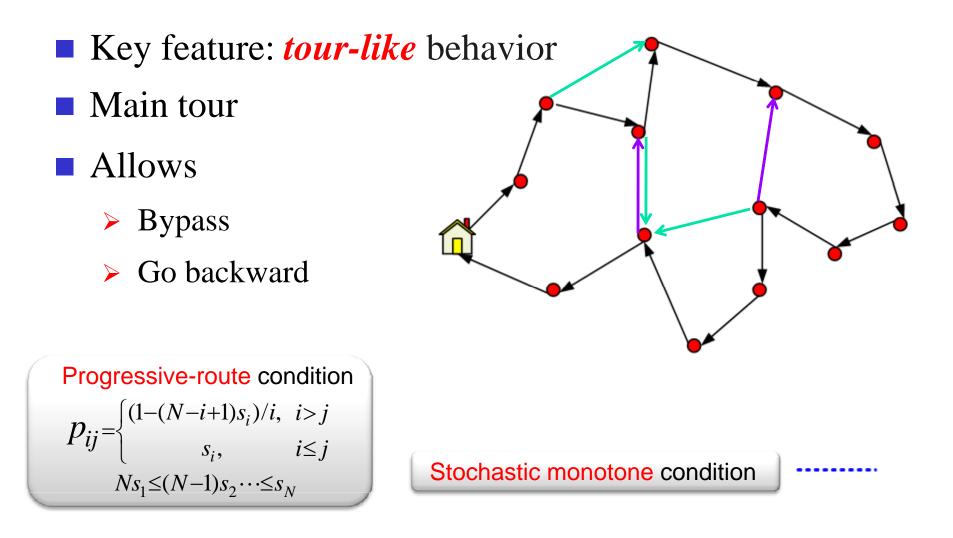
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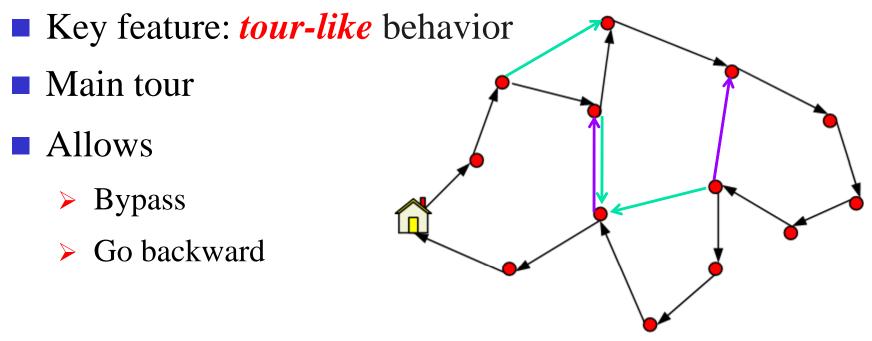








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Intuition behind complicated technical conditions: tendency of going *forwards/backwards* becomes *stronger/weaker* as time goes on

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Zero-aging class: small world

Negative-aging class: undirected (time reversibility)

Positive-aging class: tour-like

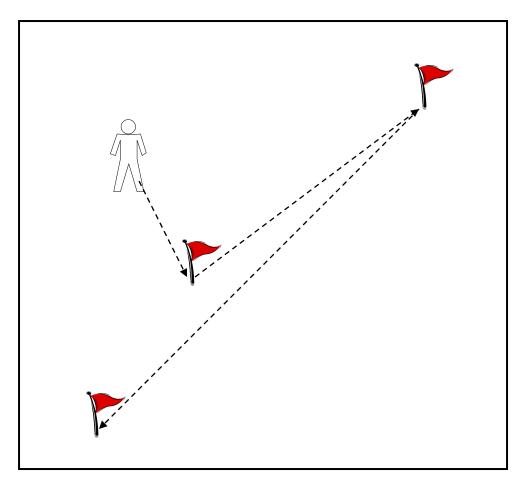




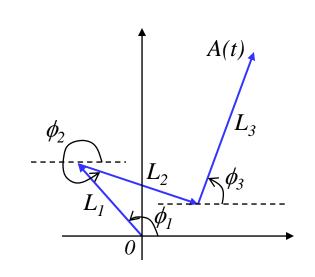
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RWP: Random Waypoint



RW: Random Walk

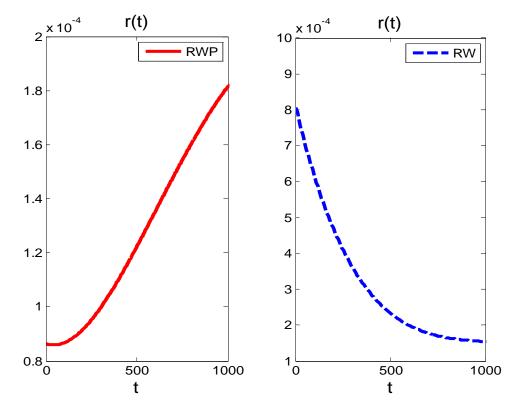


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Aging Property: RWP and RW

Characteristics of relative mobility under RWP and RW

- > RWP: biased node position/direction \rightarrow *tour-like*
- > RW: uniform node position/direction \rightarrow *time reversibility*



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Compare Two Approaches

Examples of analysis based on exponential intermeeting time assumption

M. Grossglauser and D. N. C. Tse. Mobility increases the capacity of Ad Hoc wireless networks. *ToN*, 2002.

R. Groer Z. E. KaO, and G. Koole. SIGMETRICS, 2004. aging

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Examples of analysis based on non-exponential intermeeting time



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Examples of analysis based on exponential intermeeting time assumption Examples of analysis based on non-exponential intermeeting time

What sacrifice have we made for simplicity?

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The approach based on exponential intermeeting time assumption *always underestimate* the actual network performance, under inter-meeting time with *positive aging*.





The approach based on exponential intermeeting time assumption *always underestimate* the actual network performance, under inter-meeting time with *positive aging*.

The approach based on exponential intermeeting time assumption *always overestimate* the actual network performance, under inter-meeting time with *negative aging*.

Convex Ordering of Inter-meeting Time

Inter-meeting time T vs. its exponential counterpart T_e satisfying

$$T \rightarrow \mathbb{E}\{T\} \rightarrow \mathbb{P}\{T_e \ge t\} = e^{-\frac{t}{\mathbb{E}\{T\}}}$$

$$\mathbb{E}\{\phi(T)\} \ge \mathbb{E}\{\phi(T_e)\}$$
for any convex function $\phi(\cdot)$

$$\mathbb{P}\{O > t\} = \frac{\mathbb{E}\{[T-t]^+\}}{\mathbb{E}\{T\}} \ge \frac{\mathbb{E}\{[T_e-t]^+\}}{\mathbb{E}\{T_e\}} = \mathbb{P}\{O > t\}$$
Actual delay of one-hop forwarding strategy
$$\mathbb{P}\{O > t\} = \frac{\mathbb{E}\{[T-t]^+\}}{\mathbb{E}\{T\}} \ge \frac{\mathbb{E}\{[T_e-t]^+\}}{\mathbb{E}\{T_e\}} = \mathbb{P}\{O > t\}$$

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Inter-meeting time T vs. its exponential counterpart T_e satisfying

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$$\mathbb{M} \text{ odel class 2:} \qquad T \ge cv T_e \qquad \mathbb{E}\{\phi(T)\} \ge \mathbb{E}\{\phi(T_e)\} \text{ for any convex function } \phi(\cdot)$$

$$\mathbb{P}\{D > t\} = \frac{\mathbb{E}\{[T-t]^+\}}{\mathbb{E}\{T\}} \ge \frac{\mathbb{E}\{[T_e-t]^+\}}{\mathbb{E}\{T_e\}} = \mathbb{P}\{D_e > t\}$$

$$Exp. approach gives stochastically smaller delay than the actual one}$$

> Model class 3 & 4: $T \leq_{cv} T_e$

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Is non-exponential inter-meeting time purely a disaster for MANET performance analysis and design?





Exploit the aging property can be beneficial to forwarding/routing, but incorrect use of such information is more harmful than doing nothing.



Intuition behind age-based forwarding [1,2]

➤ Essentially the same as age in mobile wireless sensor network [3,4]: smaller age → shorter distance

[1] H. Dubois-Ferriere, M. Grossglauser, and M. Vetterli. Age matters: efficient route discovery in mobile ad hoc networks using encounter ages. In *ACM MobiHoc*, Annapolis, MD, June 2003.

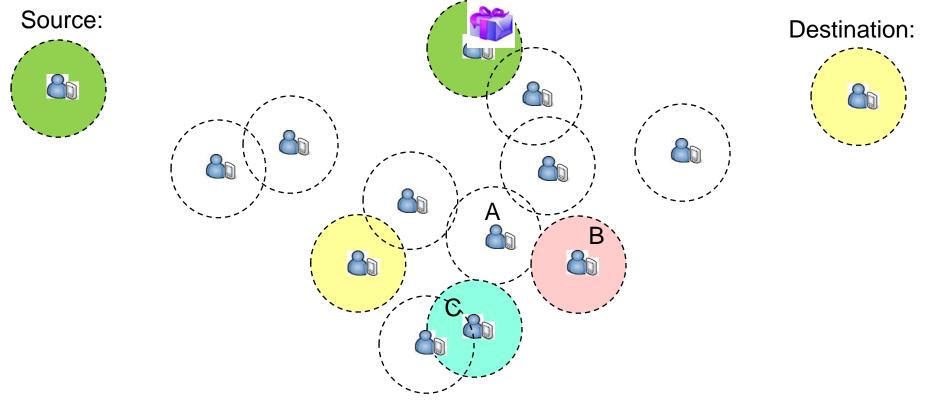
[2] T. Spyropoulos, K. Psounis, and C. S. Raghavendra. Spray and Focus: Efficient Mobility-Assisted Routing for Heterogeneous and Correlated Mobility. In *PerCom Workshops '07, White Plains, NY, 2007.*

[3] Matthias Grossglauser and Martin Vetterli. Locating nodes with ease: last encounter routing in ad hoc networks through mobility diffusion. In *IEEE Infocom*, San Francisco, March 2003.

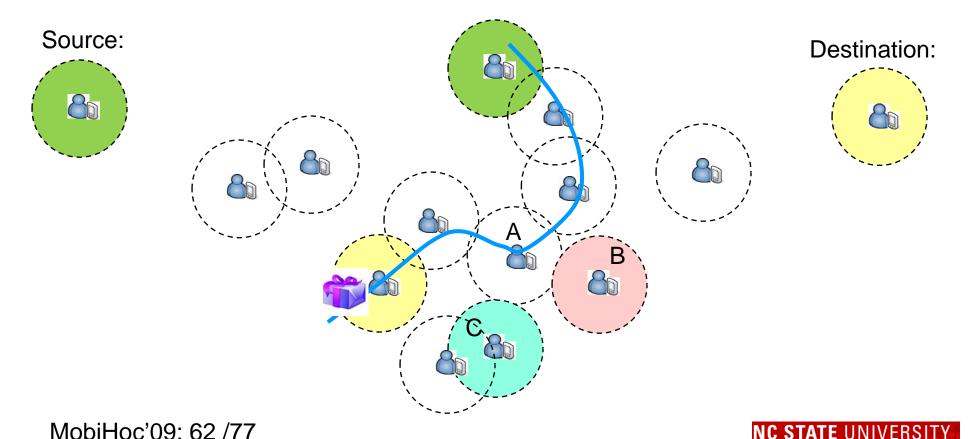
[4] Stratis Ioannidis and Peter Marbach. A brownian motion model for last encounter routing. In *IEEE Infocom, Barcelona, Spain, April 2006*.

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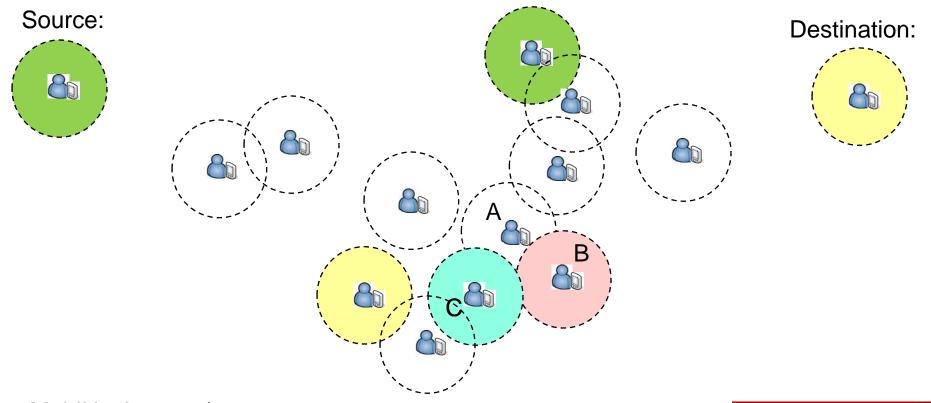
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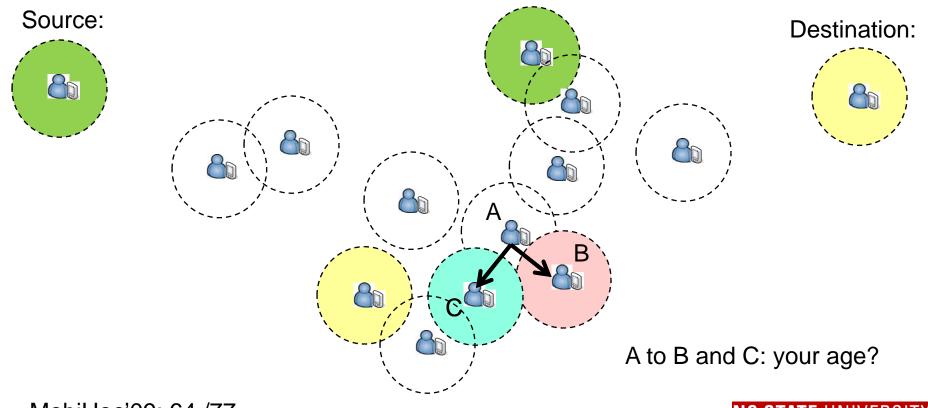


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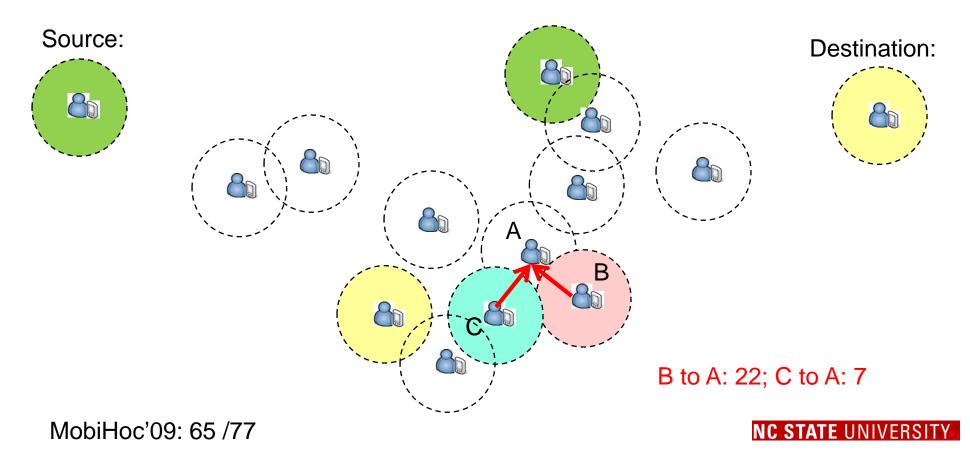
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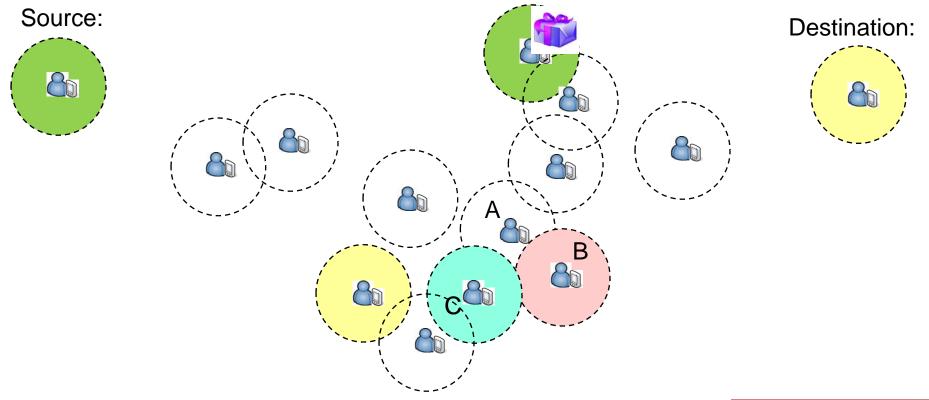
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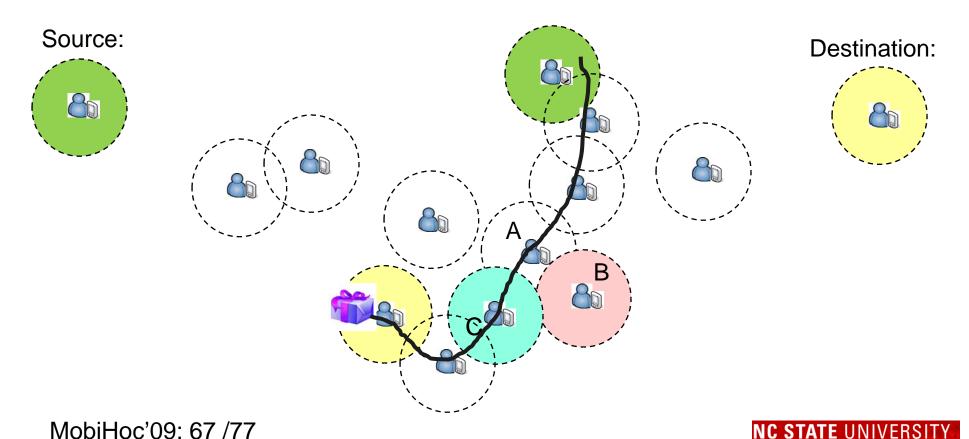
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➤ Essentially the same as age in mobile wireless sensor network [3,4]: smaller age → shorter distance



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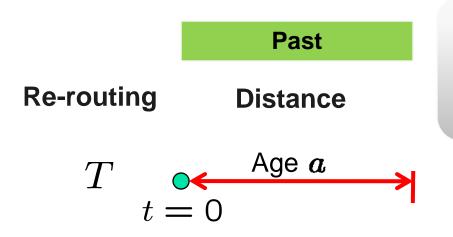
Intuition behind age-based forwarding [1,2]





Intuition: A pair of mobile nodes in *shorter distance* will meet each other in *shorter time*. Hence, mobile node with *smaller age* will meet the destination in *shorter time*.

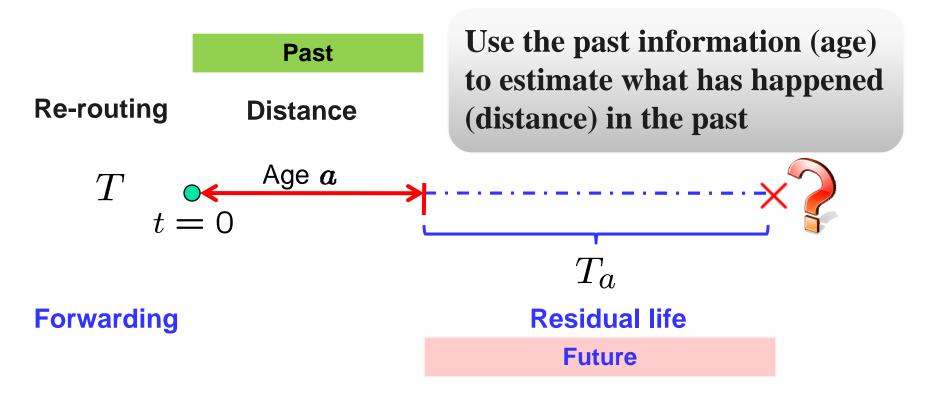




Use the past information (age) to estimate what has happened (distance) in the past







Use the past information (age) to estimate what will happen (residual life) in the future

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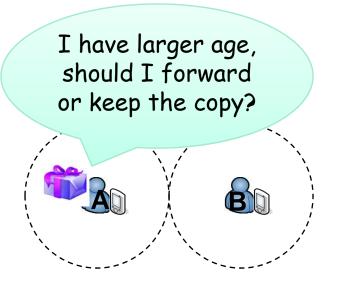


Intuition: A pair more nodes in *shorter distance* will meet each ther in *shorter time*. Hence, mobile node with smore age will meet the destination of the read of the state.

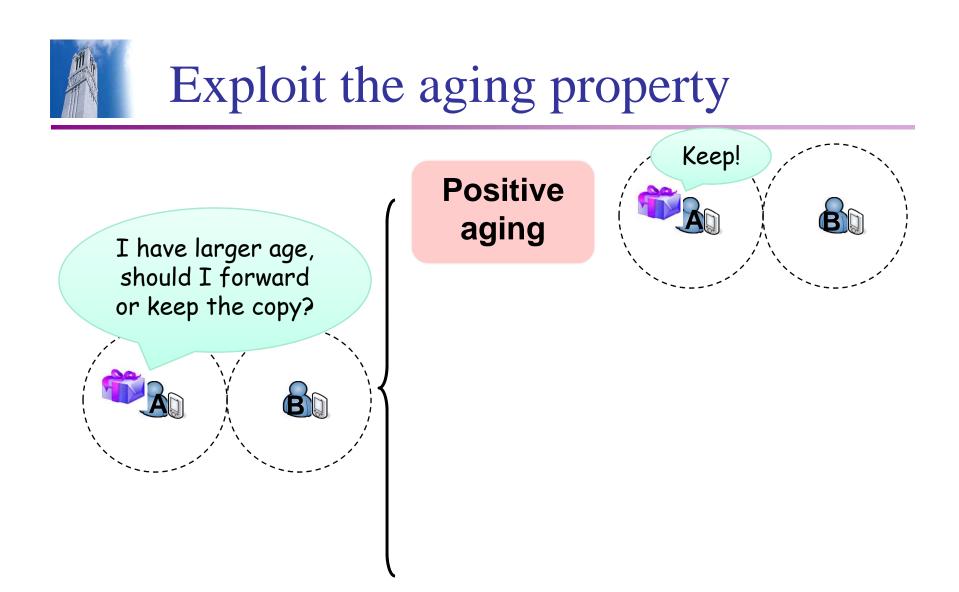


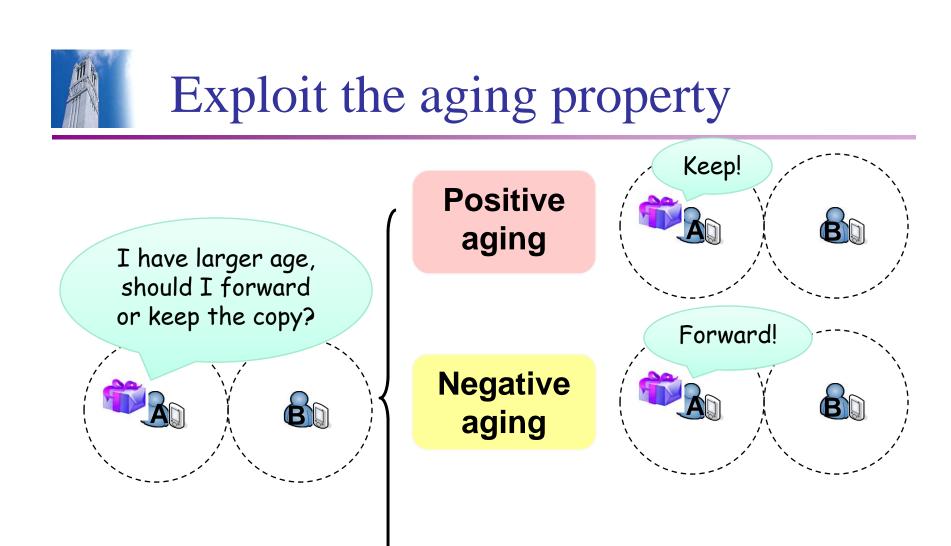


Exploit the aging property



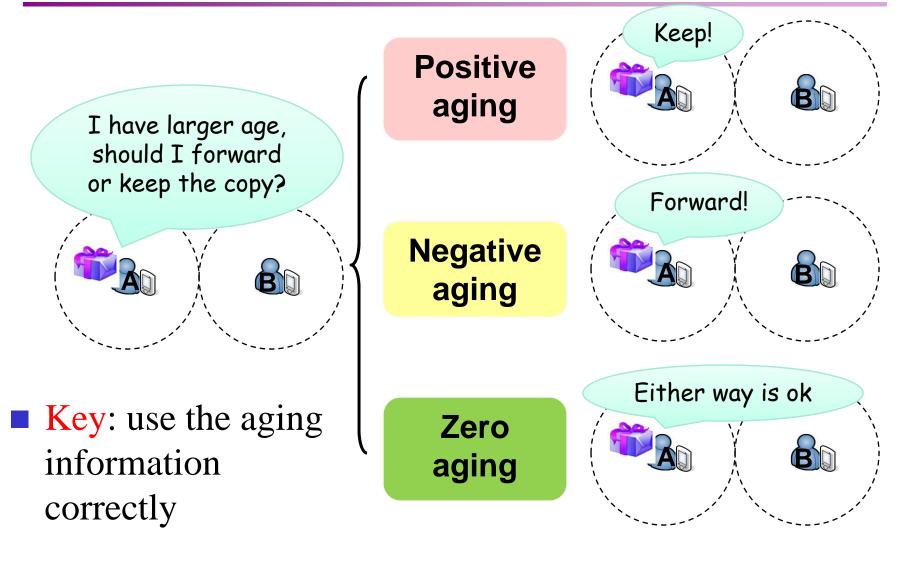








Exploit the aging property



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- Analysis: zero/negative/positive-aging models
- Aging does rule:
 - The exp. assumption based approach *always underestimate* the actual network performance, under intermeeting time with *positive aging*.
 - The exp. assumption based approach *always overestimate* the actual network performance, under intermeeting time with *negative aging*.
 - Exploit the aging property can be *beneficial* to forwarding/routing, but *incorrect* use of such information is *more harmful than doing nothing*.

Thank You!

Questions ?